

NULT New Jersey's Science & Technology University THE EDGE IN KNOWLEDGE

THE NEAR-INFRARED

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THE GOODE SOLAR **TELESCOPE**

Pour éviter une obstruction centrale qui priverait le mitroir principat d'une partie de la tumière du Salot, ce petit mitroir est situé hors de l'axe optique. Un fittre le partége de la surchauffe due à la concentration des rayons soleires.

En fonction de la région du ciel visée, des contropoids se déplacent dans ces tubes pour équilibrer le télescope et lui épargner un suiv saccade

Cet axe, aligné sur l'axe de rota de la Terre, permet au télescope de suivre le Soleit ou tout astre.

Situé à 2060 m altitude, ce lac a été la retenue d'eau la plus

grande du monde en 1884, tors de la construction du barrage. Le lac de Durs est alors devenu le grand lac de l'Ours.

L'optique adaptative

nécessite une grande puissance informatiqu pour analyser 2000 fois par seconde les déformations optiques dues à la turbulence atmospherice et commander à des miroirs déformables d'effectuer les correct

MUD DI ANIC

LE NEW SOLAR TELESCOPE

Comme la plupart des observatoires, celui-ci a des murs blancs, car cette teinte est celle qui absorbe le moins la chaleur du Soleil

séries de miroirs et entilles canalisent la ière focalisée par le tope pour l'analyse

COUPOLE MOBILE Elle tourne avec le NST pour suivre le Soleil. Elle est dotée d'un

opercule du diamètre du télescope lvoir photo p. 491

PETITS TÉLESCOPES Sous cette coupole se trouve une

nocturnes, la turbulence de l'air autou batterie de patits instruments qu de la coupole peut brouiller les images. Ces volets servent à conserver une produisent tout au long de la journée des images du Soteil en entier. Ces cliches servent à l'extérieur et l'intérieur, ce qui réduit décider quelle région de la surface solaire viser avec le NST. les mouvements de l'air

UN LAC DE HAUTE MONTAGNE

OBSERVATOIRE

AFROPOR

VERS LOS ANGELES

BARRAGE

Big Bear Lake mesure 11,2 km de long d'est en ouest et 4 km de large. Sa profondeur n'excède pas 22 m. L'observatoire solaire se trouve sur sa rive nord, à peu près à mi-distance de ses deux extrémités, À l'ouest, l routes qui le contournent se rejoignent au niveau d barrage pour aller vers Los Angeles.

REARLAKE

truite en 1972, la jet rmet d'accédera scope relie la rive nord du Big Bear Lake. alement rectiligne, elle est légérement incurvée ent de terre survenu en 1992.

Juste sous le télescope, près de son socle en béton, un spectrographe décomposi la lumière solaire dans les longueurs d'onde

Cette salle est entièrement dédiée à l'optique adaptative, qui corrige le brouillage des images par l'atmosphère terrestre, et aux instr

I LABORATOIRE SALLE DE COUDE ONTROLE SALLE DES ORDINATEURS

UN PREMIER ÉTAGE STRATÉGIQUE

Pendant les observations, les astronomes se tiennent au premier étage du bâtiment, dans la salle de contrôle, dont les fenêtres, exposées au nord, donnent sur la jetée. Ils peuvent accéder à la salle des ordinateurs adjacente, ainsi qu'au laboratoire coudé. Un escalier mène dans la coupole située deux niveaux plus haut.

Ce télescope de 1,6 m de diamètre, construit à la place d'un ancien instrument plus modeste, nous donne les images les plus précises de la surface du Soleil.



POLARIMETRY BASICS

ELECTRON IN MAGNETIC FIELD

Charged particles move in perpendicular to B field direction





STOKES PARAMETERS

180 deg. Ambiguity in linear polarization \rightarrow x2 faster angular space

Stokes vectors for linearly polarized light

Stokes vectors for circularly-polarized light





Quoted from Lites' lecture note



LINEAR POLARIZER

Absorbs one part of linear polarizations



RETARDER – ½ WAVE PLATE



RETARDER - ¼WAVE PLATE







RAINBOW



LINEAR POLARIZATION IN THE RAINBOW





Elements	wavelength	Landé g factor	$g\lambda$	Height
Fe I	6302.5	2.5	1.57	photosphere
Ca II	10830	1.22	1.32	chromosphere
Fe I	1.5648	3.0	4.69	photosphere

ZEEMAN E

Table 3.1: A list of spectral lines that have strong Zeeman splitting (Bhatnagar, 2005).

A state where energy degeneracy is broken due to magnetic field $\Delta \lambda = e/4\pi m \downarrow e \ c \ g \uparrow * \ \lambda \uparrow 2 \ B = 46.7 \ m \text{\AA} \ g \uparrow * \ (\lambda/1 \mu m \) \uparrow 2 \ (B/1000 \ G \)$



STOKES PROFILES (I, Q, U, V)

For a triplet,

Sigma component: circular polarization

Pi component: linear





MUELLER MATRIX M

A 4 \times 4 matrix that describes the polarization properties of the optics

- (I' Q' U' V')^T = M (I Q U V)^T
- If there are multiple optics in the beam train, M is the multiplication of Mueller matrix for each optical component.

• $(I Q U V)^{T} = M^{-1} (I' Q' U' V')^{T}$

NVST







TRADITIONAL SETUP



LVCR (LIQUID VARIABLE CRYSTAL RETARDER)

Voltage input to control retardation

Relatively faster modulation

Non-linear retardation vs. voltage

Temperature sensitivity



MECHANICALLY-ROTATING MODULATOR



$$\mathbf{M}_{\rm ret}(\delta) = \begin{pmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & \cos \delta & -\sin \delta \\ 0 & 0 & \sin \delta & \cos \delta \end{pmatrix}, \qquad \qquad \mathbf{R}(\theta) = \begin{pmatrix} 1 & 0 & 0 & 0 \\ 0 & \cos 2\theta & \sin 2\theta & 0 \\ 0 & -\sin 2\theta & \cos 2\theta & 0 \\ 0 & 0 & 0 & 1 \end{pmatrix}.$$

$$\mathbf{M}_{\mathbf{mod}} = \mathbf{R}(-\theta)\mathbf{M}_{\mathbf{ret}}(\delta)\mathbf{R}(\theta),$$

$$\mathbf{M_{mod}} = \begin{pmatrix} 1 & 0 & 0 & 0 \\ 0 & \cos^2 2\theta + \cos \delta \sin^2 2\theta & \cos 2\theta \sin 2\theta - \cos 2\theta \cos \delta \sin 2\theta & \sin 2\theta \sin \delta \\ 0 & \cos 2\theta \sin 2\theta - \cos 2\theta \cos \delta \sin 2\theta & \cos \delta \cos^2 2\theta + \sin^2 2\theta & -\cos 2\theta \sin \delta \\ 0 & -\sin 2\theta \sin \delta & \cos 2\theta \sin \delta & \cos \delta \end{pmatrix}$$

$$I' = \frac{1}{2} \left(I + \frac{Q}{2} ((I + \cos \delta) + (1 - \cos \delta) \cos 4\theta) + \frac{U}{2} (1 - \cos \delta) \sin 4\theta - V \sin \delta \sin 2\theta \right),$$

Double check the sign conventions

$$\mathbf{M_{mod}} = \begin{pmatrix} 1 & 0 & 0 & 0 \\ 0 & \cos^2 2\theta + \cos \delta \sin^2 2\theta & \cos 2\theta \sin 2\theta - \cos 2\theta \cos \delta \sin 2\theta & \sin 2\theta \sin \delta \\ 0 & \cos 2\theta \sin 2\theta - \cos 2\theta \cos \delta \sin 2\theta & \cos \delta \cos^2 2\theta + \sin^2 2\theta & -\cos 2\theta \sin \delta \\ 0 & -\sin 2\theta \sin \delta & \cos 2\theta \sin \delta & \cos \delta \end{pmatrix}.$$

MODULATION

Modulated intensity after passing through analyzer:

- $\delta = 127$ gives the same modulation $I' = \frac{1}{2} \left(I + \frac{Q}{2} ((I + \cos \delta) + (1 \cos \delta) \cos 4\theta) + \frac{U}{2} (1 \cos \delta) \sin 4\theta V \sin \delta \sin 2\theta \right)$ amplitude for Q, U, V.
- Dividing modulation by 8 segments then applying different combination gives different Stokes parameters.



Parameter	Combination	
I	1+2+3+4+5+6+7+8	
Q	1-2-3+4+5-6-7+8	
U	1+2-3-4+5+6-7-8	
V	-1-2-3-4+5+6+7+8	

SYNCHRONIZATION BETWEEN MODULATOR & CAMERA

Modulation is a function of time, 8 segments mean 8 frames from camera.

• The timing of the camera exposure should match with the rotation of the modulator.

Controlling modulator from the camera signal is difficult.

Triggering camera exposure from the modulator gives exposure timing error.

COMPROMISE: MATCHING MODULATION RATE,





The modulator rotates at a fixed rate, the camera's exposure time is determined at the same rate.

The camera continuously takes image when it is on. Modulator initializes when software initialzes

• The phase of the modulator is random w.r.t. the framing.

TROUBLES WITH RANDOM

PHASE OFFSET Simply combining the 8 segments by the combination rule assumes that the 1st frame start at 0 modulation angle. Random phase offset moves the starting position to any angle between 0 & 360°.

Q & U mixture: Q, U have the same period different phase. With offset $\phi=22.5^{\circ}$, U signal will look as Q signal.

Each segment from pure Q, U, V modulation only have single sign. With a random phase, some segment will contain both signs. \rightarrow signal reduction by cancellation



READOUT TIMING ISSUE



RIPPLE READOUT OF CMOS DETECTORS







CROSSTALK & EFFICIENCY LOSS DUE TO Φ

Modulation signal

$$I' = \frac{1}{2} \left(I + \frac{Q}{2} ((I + \cos \delta) + (1 - \cos \delta) \cos 4\theta) + \frac{U}{2} (1 - \cos \delta) \sin 4\theta - V \sin \delta \sin 2\theta \right)$$

RESTORING THE ORIGINAL SIGNAL

$$\begin{bmatrix} I \\ Q \\ U \\ V \end{bmatrix} = \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & \cos 4\varphi & \sin 4\varphi & 0 \\ 0 & -\sin 4\varphi & \cos 4\varphi & 0 \\ 0 & 0 & 0 & \sec 2\varphi \end{bmatrix} \begin{bmatrix} I' \\ Q' \\ U' \\ V' \end{bmatrix}$$

 $\boldsymbol{\varphi}$ information is stored in a text file for every burst.

• If $|\phi| > 11.25^{\circ}$, the following sign convention table shifts accordingly so that $-11.25 \le \phi < 11.25$.

Parameter	Camera 1	Camera 2	
I	++++++++	+++++++++	
Q	+ + + +	-++++-	
U	++++	++++	
V	+++++	+ + + +	



INFRARED IMAGING MAGNETOGRAPH (IRIM)

Fabry-Perot based, wavelength scanning magnetograph

Spatial resolution: 0.2" at Fe I 1.56 µm

Bandwidth: 0.1 Å

Temporal resolution: 50 secs

Dual-beam imaging

Field of view: 50" x 25"





IRIM COMPONENTS

Modulator

- Mechanically rotating birefringent polymer
- 5" aperture, 2" thickness

Analyzer

Two Wollaston prisms (40 mm x 40 mm)

Camera

- CMOS camera w/ ripple readout
- Maximum 30 fps, optimal at 20 fps







M4-M6

Dec rotation between M3 & M4

RA rotation between M4 & M5



IRIM BEAM PATHS

Two Wollaston prisms

Prefilter: FWHM 25 A

Lyot: FWHM 2.5 A

- $\hfill Tilted$ by ${\sim}45$ deg. due to intrinsic linear polarizer
- Transmission: 0.1
- To be replaced to another F-P

F-P: FWHM 0.1 A





CAMERA

Manufacturer: Rockwell

1024×1024, 14 bit HgCdTe CMOS

Max 30 fps

 $1k \times 1k$ chip is divided by two halves to accommodate dual beams with different polarizations.


OPERATION OF WAVEPLATE & CAMERA Waveplate rotates with 1 rps.

Computer

Camera

(1 - 16)

Waveplate

Controller

F-P

Camera is free running, collecting frames in the frame grabber.

16 successive signals

After one rotation, wavelength tuning of F-P and data retrieval to computer occur.

17th frame will be discarded.

From the 18th frame, the second burst begins.

13 wavelength sampling, 221 frames per burst

ERROR ESTIMATE



Possible sources of noise

- Poisson noise
- Readout noise (75e- per frame)
- Seeing-induced crosstalk
- Instrumental residual crosstalk

Total error estimate

- 3x10⁻³ Ic for vector magnetograph (1 rps of waveplate rotation)
- 1.5x10⁻³ lc for longitudinal field measurement (4 rps)

FIRST LIGHT

Under poor seeing, single beam, LCVRs

Exp: 90 ms

14/160 * 1.56/0.63=0.21



DUAL-BEAM TEST



50/160 * 1.56/0.58 = 0.84



Hinode/FG

IRIM

PORE UNDER FAIR SEEING



NETWORK UNDER GOOD SEEING



COMPARISON WITH HMI









HIGH RESOLUTION POLARIMETRY





IRIM



06/04/2012



NIRIS (NEAR-INFRARED IMAGING SPECTROPOLARIMETER)

- Dual-beam imaging for minimal seeing crosstalk
- Field of view: 85" round
- Modulator: 2 rev/s
- Cadence: 40 s for 60 wv
- Accuracy: 10 G for B₁ and 100 G for B₁

Observe 6 hrs per day throughout the year with many good seeing days!





SPECTROGRAPH VS. FILTER IMAGING

FISS



HIGH SPATIAL RESOLUTION W/ WIDER FIELD Diffraction 19.25 arcsec

Typical resolution: 0.35 arcsec





IRIM



HIGH SPECTRAL RESOLUTION

Spectral bandwidth: 0.01 nm

Spectral sampling: typically 30-60 wavelengths, but flexible



Fig. 5 Stokes profiles before and during the flare. Stokes components (I, Q, U, and V) taken near R3 before (blue) and during (pink) the flare. a Stokes I. b Stokes Q. c Stokes U. d Stokes V. It is clear that the Stokes I and V components remain almost unchanged but Q and U components are significantly affected during the flare

HIGH TEMPORAL RESOLUTION

Temporal resolution: 25-45 secs, depending on the choice of wavelength sampling



DOLLERGRAM



5 min oscillation?





NIRIS LAYOUT







DATA PROCESSING & POLARIZATION CALIBRATION

DATA PROCESSING PROCEDURES

- Align frames w/ features
- Align dual beams
- Subtract dual beams w/ de-stretch (registration)
- Combine 16 frames to create initial Stokes profiles
- Correct for phase offset between modulator & detector
- Calibrate instrumental crosstalk



FLAT PATTERN

• ROI selection by default (720 x 720 pixels)



NIRIS DATA FILES

- cals_150903_202039.fts: Stokes I, Q, U, and V maps
- fout150903_185524.sav: an IDL binary file that includes some calibration parameters
- snap_150903_173945: snapshot images of the Stokes maps near the line center
- nirisinv_YYMMDD_HHMMSS: ME inversion files

SIGNIFICANT RESIDUAL CROSSTALK



FITS HEADER OF CALS .

- REFWV: the wavelength corresponding to the line center.
- STARTWV: a relative offset of wavelength from the REFWV
- ENDWV: a relative offset of wavelength from the REFWV
- INCWV: a change in wavelength for each scan step. Unit is in Angstrom.
- LCEN: This is a calculated round-up line center index in wavelength sampling sequence
- The COMMENT and HISTORY lines
- NAXIS1,2,3,4 : Each FITS file is a fourdimensional data (I, Q, U, V)
- Plot, img[255,255,*,1]

	x
File	
Line SIMPLE = T / Written by IDL: Wed Dec 14 02:04:05 2016 BITPIX = 16 / data type of original image NAXIS = 4 / dimension of original image NAXIS1 = 720 /Number of positions along axis 1 NAXIS2 = 720 /Number of positions along axis 2 NAXIS3 = 60 /Number of positions along axis 3 NAXIS4 = 4 /Number of positions along axis 4 CTYPE1 = 'E-W ARCS' CRVAL1 = CRVAL1 = 0 CRVAL2 = 0 CRPIX1 = 1024 CDELT1 = 0.0244140625000 / image scale arcsec/pixel CDELT2 = 0.0244140625000 / image scale arcsec/pixel XCEN = 'refer to bbso log at http://www.bbso.njit.edu/cgi-bin/logs' / YCEN = 'same as above' / ORIGIN = 'BSO' / Big Bear Solar Observatory INSTRUME= 'nins' / NIRIS with Teledyne camera TELESCOP= 'NST ' / NST Coude room TARGET = 'NOAA 12409' IMAGETYP= Image' EXPOSURE= SOLAR_P0= 0. / COD temperature, C DATE - 2015-09-03T20:20:39' / image acquisition date and time UT DATE-OBS= '2015-09-03' / UTC YYYY-MM-DD TIME-OBS= '2015:09-03' / UTC YYYY-MM-DD TIME-OBS= '2012:03:03	

SPECTRAL PROFILES





CALIBRATION

Sources of magnetic signal errors (crosstalk)

- Image motion due to seeing
 - Faster modulation reduces seeing-induced crosstalk
 - Longer wavelength has less contamination.
- Crosstalk due to optical components
 - Mirror surface can function as both retarder & linear polarizer.
 - Retardation proportional to ϑ^2

SEEING-INDUCED CROSSTALK

Single beam : To measure Stokes V with I+V at t1 and I-V at t2

Intensity fluctuation due to image motion – bigger that pol. signals



Figure 3.5: Crosstalk level compared to the line continuum according to the rotation speed of retarder and the amount of beam imbalance between two cameras (Judge et al., 2004; Elmore, 2006). The beam imbalance of 100% signifies single beam.

DUAL BEAM TO MINIMIZE

	Status Position Frames per Z step Image type: 1 Average Modes of operation Addtl. information Observer: Image type: Image type:
Intensity at cursor position Image statistics	Start Stop IV Save files Take dark # of frames 50 Burst start Test plot Status

RIPPLE READOUT OF CMOS DETECTORS







CALIBRATION OF INSTRUMENTAL CROSSTALK: MUELLER describes the

- polarization properties of the optics
 - $(I' Q' U' V')^{\mathsf{T}} = \mathsf{M} (I Q U V)^{\mathsf{T}}$
- If there are multiple optics in the beam train, M is the multiplication of Mueller matrix for each optical component.
 - $M = M_n M_{n-1} M_{n-2} \dots M_3 T$
 - $(I Q U V)^{T} = M^{-1} (I' Q' U' V')^{T}$
 - \sim 20 mirror elements function as a quarter-wave plate!

- Mueller matrix of a single mirror
- r_s/r_p : reflectivity ratio between parallel & perpendicular light
- δ : retardation



Elmore 2011

CALIBRATION OF T (TELESCOPE)

 $\mathsf{T}=\mathsf{M}_2\;\mathsf{M}_1$

Off-axis geometry creates non-zero polarization

Average incident angle of GST - 12 deg.

Simulation performed by S. Yuan

Our conclusion : T is not significant



Figure 3.6: Calibration of a telescope by sub-aperture method (Socas-Navarro, 2005; Elmore, 2006). A calibration unit that is smaller than the aperture of the telescope sweeps over the aperture to measure crosstalk at a sub-field, while a mask behind the secondary mirror blocks the beam that does not pass through the calibration optics.

SIMULATING M FOR THE YEAR: GROUPING OPTICAL ELEMENTS often.

- Proposed by D. Elmore
- Dec rotation between M3 & M4
- HA rotation between M4 & M5
- Add a coordinate-breaking matrix at every fast-axis change
- M (dec,ha)=M_{rest} R(φ₃,ha) M₄ R(φ₂,dec) M₃ R(φ₁) T
- M over different HA and DEC are measured.



FINDING M_{REST} THAT IS INVARIANT OVER DEC & HA

- Assumption: T and relay optics are mature (no rapid bulid-up of oxidized coating).
 - $M (dec,ha) = M_{rest} R(\phi_3,ha) M_4 R(\phi_2,dec) M_3 R(\phi_1)$
 - When passing through the linear polarizer, the information of T does not transmit in most cases.
- $M_{rest} = M [R(\phi_3,h\alpha) M_4 R(\phi_2,dec) M_3 R(\phi_1)]^{-1}$ = constant
 - \rightarrow Invariant over whole time of the year, ideally.
- Find the combination of M_3 & M_4 properties (r_s/r_p , δ) that makes M_{rest} nearly constant possible
- Minimum standard deviation of data points
M_{REST}

- Get the combination of $M_3 \& M_4$ properties that minimizes deviation of $M_{\rm rest}$ through least square fitting
 - $r_s/r_p = -0.004$
 - δ_{M3}=-25°
 - δ_{м4}=-27°
- Determine M_{rest} , then multiply with $R(\phi_3,h\alpha) M_4 R(\phi_2,dec) M_3 R(\phi_1)$ to get M for any day of year

BETTER WAY – MULTI-PARAMETER FITTING FROM MULTIPLE MEASUREMENTS

 $\mathbf{s}_{\mathbf{I}} = \mathbf{X} \mathbf{U} \mathbf{C} \mathbf{s}_{t} + \mathbf{b}$

(1)

where Measured instrument vector $\mathbf{SI}(x,y,\lambda)$ \equiv $\mathbf{X}(x,y,\lambda)$ Polarimeter response matrix \equiv Unknown sample Mueller matrix $\mathbf{U}(x,y,\lambda) \equiv$ $\mathbf{C}(x, y, \lambda) \equiv$ Calibration optics configuration Mueller matrix $\mathbf{s}_{\mathbf{t}}(x, y, \lambda) \equiv$ Lamp Stokes vector (historically the telescope vector) \equiv Instrument bias vector $\mathbf{b}(x,y)$

 $x \equiv$ Horizontal spatial dimension

 $y \equiv Vertical spatial dimension$

 $\lambda \equiv Wavelength$

Without the sample in the beam but with a series of polarization configurations, sufficient measurements of the instrument vector are collected to allow the **X** matrix to be calculated as described in the next sections. The same measurements are repeated with the unknown sample in the beam and a new polarimeter response matrix, X' = XU, is calculated. The unknown sample Mueller matrix is then $U = X^{-1}X'$.

NCAR Technical Note NCAR/TN-355+STR, A Calibration Technique for the Advanced Stokes Polarimeter, September, 1990.

CALIBRATION OF INSTRUMENTAL





MODULATION W/ 12 HR PERIOD 06/06/12





08/30/11



09/06/11



09/13/12





10/06/11



10/08/12





M_REST FROM 06/27/2012



M REST FROM 10/01/2012 A Carlos

MEASURED VS. SIMULATED FROM M_REST

Calibration of 06/27 from the M_{rest} on 10/01





INDIRECT CALIBRATION



Kuhn et al. 1994

Contamination from the other Stokes parameters – breaking symmetry/anti-symmetry of spectral profiles





2

SECOND ORDER CALIBRATION

Subtract asymmetric contamination in Q, U

Subtract Q, U contribution from V



NIRIS STOKES PROCESSING REQUIREMENTS

IDL with astro package

Mpfit

A couple of files we made

Fitsio for uncompressing

8 gb < memory space

4 < CPU cores

• For inversion, the more the better.



STOKES INVERSION TECHNIQUES

STOKES INVERSION

Fitting the model profiles into the measured profiles

The model profiles are outcome of physical parameters

The more the parameters, the more accurate fitting works, but harder to trust.

Milne-Eddington approximation

SIR – the most robust method probably for photospheric lines

STiC – non-LTE lines

Hazel – best for He 10830

And so on...

MILNE-EDDINGTON APPROXIMATION

The simplest inversion

Assumption:

1. There is no velocity gradient over optical depth – symmetric profiles

2. The source function is the 1st order polynomial over optical depth Pros:

- 1. Analytical solution
- 2. Faster processing

Cons:

- 1. Cannot fit asymmetric profiles only good for photospheric lines
- 2. Limited parameter outputs

The solutions of these equations are given by

 $I - V = I_0(\lambda + g^* \lambda_B)$

where $I_0(\lambda)$ is the solution of the equation

$$\frac{dI_0}{I_0} = (1 + \eta_0 \phi_0)(I_0 - B_T) \; .$$

We define the center of gravity for I + V by

$$_{+} = \frac{\int (I_c - (I+V))\lambda d\lambda}{\int (I_c - (I+V))d\lambda}$$
(31)

(308)

(309)

and that for I - V by

$$\lambda_{-} = \frac{\int (I_c - (I - V))\lambda d\lambda}{\int (I_c - (I - V))d\lambda}$$
(3)

where I_c is the continuum intensity. Suppose I_0 is symmetric about $\lambda_0,$ then the relations will hold

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$$\lambda_{\pm} = \lambda_0 \pm g^* \lambda_B \tag{313}$$

so that we obtain

$$B_{\parallel} = \frac{1}{\alpha \alpha} (\lambda_{+} - \lambda_{-}). \quad (314)$$

This expression holds even for inclined field, and does not suffer from the saturation effect.

5.3. Milne-Eddington Solution

$$\frac{d\boldsymbol{I}}{d\tau} = \mathbf{K}(\boldsymbol{I} - B_T \boldsymbol{U})$$

where I = (I, Q, U, V) and U = (1, 0, 0, 0).

Assumptions:

- 1. K is constant over τ .
- 2. $B_T = B_0 + B_1 \tau$

$$\frac{d}{d\tau}\left[-\frac{1}{4}v_B^2\frac{\partial^2 I_0}{\partial v^2}\sin^2\theta\cos 2\chi\right] = -\eta_0\frac{1}{4}v_B^2\frac{\partial^2 \phi_0}{\partial v^2}\sin^2\theta\cos 2\chi(I-B_T) \quad (296)$$

$$-\frac{1}{7}v_B^2(1+\eta_0\phi_0)\sin^2\theta\cos 2\chi\frac{\partial^2 I_0}{\partial v^2}, \quad (297)$$

We thus obtain

$$Q = -\frac{1}{4}v_{\beta}^{2}\frac{\partial^{2}I_{\beta}}{\partial v^{2}}\sin^{2}\theta\cos 2\chi \qquad (298)$$
and in the same way

$$U = -\frac{1}{4}v_{\beta}^{2}\frac{\partial^{2}I_{\alpha}}{\partial v^{2}}\sin^{2}\theta\sin 2\chi . \qquad (299)$$

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Finally we obtain simpler expressions

$$\beta_{\perp} \propto \frac{\sqrt{Q^2 + U^2}}{I}$$
 (300)
 $\chi = \frac{1}{2} \tan^{-1} \frac{U}{Q}$ (301)

5.2. Center-of-gravity method

Suppose magnetic field is aligned with the line of sight: $\theta=0.$ Then we have $\eta_Q=\eta_U=\rho_Q=\rho_U=0,$ and

$$\frac{II}{l\tau} = \eta_I (I - B_T) + \eta_V V \qquad (302)$$

$$\frac{V}{V} = \eta_V (I - B_T) + \eta_I V \qquad (303)$$

which looks the same as the form derived from the first order weak field approximation. From these we obtain

$$\frac{d}{d\tau}(I + V) = (\eta_I + \eta_V)(I + V - B_T) \qquad (304)$$

$$\frac{d}{d\tau}(I - V) = (\eta_I - \eta_V)(I - V - B_T) \qquad (305)$$

or explicitly

$$\frac{d}{d\tau}(I + V) = (1 + \eta_0 \phi_r)(I + V - B_T) \qquad (306)$$

$$\frac{d}{d\tau}(I - V) = (1 + \eta_0 \phi_b)(I - V - B_T). \qquad (307)$$

		11
		MH .
- 34 -		- 35 -
Assume a solution of the form		T
$I=I_0+I_1 au$	(316)	
		$\psi_p = L(a, v)$ $\psi_p = L(a, v)$
$\boldsymbol{I}_1 = \mathbf{K} (\boldsymbol{I}_0 - B_0 \boldsymbol{U} + \tau (\boldsymbol{I}_1 - B_1 \boldsymbol{U}))$	(317)	$\psi_r = L(u, v = v)$ $\psi_b = L(u, v + v)$
		4
$egin{array}{rcl} I_1 &= B_1 U \ I_0 &= B_0 U + B_1 \mathbf{K}^{-1} U \end{array}$	(318) (319)	$\eta_I = 1 + \eta_0 \frac{1}{2} \left[\phi_p \sin^2 \theta + \frac{\phi_b + \phi_b}{2} \right]$
		$\eta_Q = \eta_0 \frac{1}{2} \left[\phi_p - \frac{\phi_b + \phi_r}{2} \right] \sin^2$
$I = B_0 + B_1 K_{ii}^{-1} = B_0 + B_1 [n_i (n_i^2 + \rho_0^2 + \rho_{ii}^2 + \rho_{ii}^2)] / \Delta$	(320)	$1 \begin{bmatrix} 2 \\ \phi_b + \phi_r \end{bmatrix}_{\text{cin}^2}$
$Q = B_1 K_{q_1}^{-1} = -B_1 [\eta_l^2 \eta_Q + \eta_l (\eta_V \rho_U - \eta_U \rho_V) + \rho_Q (\eta_Q \rho_Q + \eta_U \rho_U + \eta_V \rho_V)] / \Delta$	(321)	$\eta_0 = \eta_0 \frac{1}{2} \left[\phi_p - \frac{1}{2} \right] \sin \theta$
$U = B_1 K_{ui}^{-1} = -B_1 [\eta_I^2 \eta_U + \eta_I (\eta_Q \rho_V - \eta_V \rho_Q) + \rho_U (\eta_Q \rho_Q + \eta_U \rho_U + \eta_V \rho_V)] / \Delta$	(322)	$\eta_V = \eta_0 \frac{1}{2} [\phi_r - \phi_b] \cos \theta$
$V = B_1 K_{vi}^{-1} = -B_1 [\eta_I^2 \eta_V + \eta_I (\eta_U \rho_Q - \eta_Q \rho_U) + \rho_V (\eta_Q \rho_Q + \eta_U \rho_U + \eta_V \rho_V)] / \Delta$	(323)	$\rho_Q = \eta_0 \frac{1}{2} \left[\psi_p - \frac{\psi_b + \psi_r}{2} \right] \sin^2$
here $\Delta = \eta_I^2 [\eta_I^2 - \eta_Q^2 - \eta_U^2 - \eta_V^2 + \rho_Q^2 + \rho_U^2 + \rho_V^2] - (\eta_Q \rho_Q + \eta_U \rho_U + \eta_V \rho_V)^2$.		$\alpha_{\mu} = n \frac{1}{2} \left[\psi_b + \psi_r \right] \sin^2 \theta$
Free parameters: B , θ , χ , η_0 , λ_D , a , λ_0 , B_0 , B_1 .		$p_U = \eta_0 \frac{1}{2} \begin{bmatrix} \psi_p - \frac{1}{2} \end{bmatrix} \sin \frac{1}{2}$
		$\rho_V = \eta_0 \frac{1}{2} [\psi_r - \psi_b] \cos \theta$
5.3.1. Formulations for computation		5.
inctional values		$\Delta = \eta_I^2 [\eta_I^2 - \eta_Q^2 - \eta_U^2 - \eta_V^2 + \rho_Q^2 + \rho_U^2 + \rho_V^2] - \eta_U^2 + $
1. Free parameters: B , θ , χ , η_0 , λ_D , a , λ_0 , B_0 , B_1 among which B , η_0 , λ_D , a , B_0 ,	B_1 are	6.
positive dennite:		$I = B_0 + B_1 [\eta_l (\eta_l^2 + \rho_Q^2 + \rho_U^2 + \rho_V^2)] / 2$
2. $u = \frac{\lambda - \lambda_0}{\lambda_0}$	(324)	$Q = -B_1[\eta_1^2\eta_Q + \eta_I(\eta_V\rho_U - \eta_U\rho_V) + \rho_I U]$ $U = -B_2[\eta_2^2\eta_V + \eta_I(\eta_V\rho_U - \eta_U\rho_V) + \rho_I(\eta_U\rho_U) - \eta_V\rho_I) + \rho_I(\eta_U\rho_U) + \rho_I(\eta_U$
$c = \frac{\Delta \lambda_D}{B}$	(024)	$V = -B_1[\eta_l^2\eta_V + \eta_l(\eta_U\rho_Q - \eta_Q\rho_U) + \rho_l$
$v_B = c_0 \frac{B}{\Delta \lambda_D}$	(325)	
3.		Partial derivative over η_l
$\phi_p = H(a, v)$	(326)	$\frac{\partial I}{\partial t} = B_1 (3p_1^2 + p_2^2 + p_1^2 + p_2^2) / c_1^2$
$\phi_r = H(a, v - v_B)$	(327)	
$\phi_b = H(a, v + v_B)$	(328)	$\overline{\partial \eta_Q}$

	$\psi_r = L(a, v - v_B)$	(330)
	$\psi_b = L(a, v + v_B)$	(331)
	11 040 1	
η_I	$= 1 + \eta_0 \frac{1}{2} \left[\phi_p \sin^2 \theta + \frac{\phi_b + \phi_r}{2} (1 + \cos^2 \theta) \right]$	(332)
η_Q	$= \eta_0 \frac{1}{2} \left[\phi_p - \frac{\phi_b + \phi_r}{2} \right] \sin^2 \theta \cos 2\chi$	(333)
η_U	$= \eta_0 \frac{1}{2} \left[\phi_p - \frac{\phi_b + \phi_r}{2} \right] \sin^2 \theta \sin 2\chi$	(334)
η_V	$= \eta_0 \frac{1}{2} [\phi_r - \phi_b] \cos \theta$	(335)
ΡQ	$= \eta_0 \frac{1}{2} \left[\psi_p - \frac{\psi_b + \psi_r}{2} \right] \sin^2 \theta \cos 2\chi$	(336)
ρυ	$= \eta_0 \frac{1}{2} \left[\psi_p - \frac{\psi_b + \psi_r}{2} \right] \sin^2 \theta \sin 2\chi$	(337)
ρ_V	$= \eta_0 \frac{1}{2} [\psi_r - \psi_b] \cos \theta$	(338)
$\eta_I^2 [\eta_I^2 - \eta_Q^2 -$	$\eta_U^2 - \eta_V^2 + \rho_Q^2 + \rho_U^2 + \rho_V^2] - (\eta_Q \rho_Q + \eta_U \rho_U + \eta_V \rho_V)^2$	(339)

Ι	=	$B_0 + B_1 [\eta_I (\eta_I^2 + \rho_Q^2 + \rho_U^2 + \rho_V^2)] / \Delta$	(340)
Q	=	$-B_1[\eta_I^2\eta_Q + \eta_I(\eta_V\rho_U - \eta_U\rho_V) + \rho_Q(\eta_Q\rho_Q + \eta_U\rho_U + \eta_V\rho_V)]/\Delta$	(341)
U	=	$-B_1[\eta_I^2\eta_U + \eta_I(\eta_Q\rho_V - \eta_V\rho_Q) + \rho_U(\eta_Q\rho_Q + \eta_U\rho_U + \eta_V\rho_V)]/\Delta$	(342)
V	=	$-B_1[\eta_I^2\eta_V + \eta_I(\eta_U\rho_Q - \eta_Q\rho_U) + \rho_V(\eta_Q\rho_Q + \eta_U\rho_U + \eta_V\rho_V)]/\Delta$	(343

$$= B_1(3\eta_I^2 + \rho_Q^2 + \rho_U^2 + \rho_V^2)/\Delta - (I - B_0)\frac{\partial \Delta}{\partial \eta_I}/\Delta \qquad (344)$$

$$\frac{\partial I}{\partial \eta_Q} = -(I - B_0)\frac{\partial \Delta}{\partial \eta_Q}/\Delta \qquad (345)$$

$$\eta_I = 1 + \eta_0 \frac{1}{2} \left[\phi_p \sin^2 \theta + \frac{\phi_b + \phi_r}{2} (1 + \cos^2 \theta) \right]$$

$$\eta_0 = \eta_0 \frac{1}{2} \left[\phi_p - \frac{\phi_b + \phi_r}{2} \sin^2 \theta \cos^2 \chi \right]$$

$$\rho_V = \eta_0 \frac{1}{3} [\psi_r - \psi_b] \cos \theta$$

$rac{\partial I}{\partial \eta_U} = -(I - B_0) rac{\partial \Delta}{\partial \eta_U} / \Delta$	(346
$rac{\partial I}{\partial \eta_V} = -(I - B_0) rac{\partial \Delta}{\partial \eta_V} / \Delta$	(347
$\frac{\partial I}{\partial \rho_Q} = B_1 (2\eta_I \rho_Q) / \Delta - (I - B_0) \frac{\partial \Delta}{\partial \rho_Q} / \Delta$	(348
$rac{\partial I}{\partial ho_U} = B_1 (2\eta_I ho_U) / \Delta - (I - B_0) rac{\partial \Delta}{\partial ho_U} / \Delta$	(349
$\frac{\partial I}{\partial \rho_V} = B_1 (2\eta_I \rho_V) / \Delta - (I - B_0) \frac{\partial \Delta}{\partial \rho_V} / \Delta$	(350
$\frac{\partial Q}{\partial \eta_I} = -B_1 [2\eta_I \eta_Q + (\eta_V \rho_U - \eta_U \rho_V)] / \Delta - Q \frac{\partial \Delta}{\partial \eta_I} / \Delta$	(351
$\frac{\partial Q}{\partial \eta_Q} = -B_1 [\eta_I^2 + \rho_Q^2] / \Delta - Q \frac{\partial \Delta}{\partial \eta_Q} / \Delta$	(352
$\frac{\partial Q}{\partial \eta_U} = -B_1 [-\eta_I \rho_V + \rho_Q \rho_U] / \Delta - Q \frac{\partial \Delta}{\partial \eta_U} / \Delta$	(353
$\frac{\partial Q}{\partial \eta_V} = -B_1 [\eta_I \rho_U + \rho_Q \rho_V] / \Delta - Q \frac{\partial \Delta}{\partial \eta_V} / \Delta$	(354
$\frac{\partial Q}{\partial \rho_Q} = -B_1 [2\eta_Q \rho_Q + \eta_U \rho_U + \eta_V \rho_V] / \Delta - Q \frac{\partial \Delta}{\partial \rho_Q} / \Delta$	(355
$\frac{\partial Q}{\partial \rho_U} = -B_1 [\eta_l \eta_V + \rho_Q \eta_U] / \Delta - Q \frac{\partial \Delta}{\partial \rho_U} / \Delta$	(356
$\frac{\partial Q}{\partial \rho_V} = -B_1 [-\eta_I \eta_U + \rho_Q \eta_V] / \Delta - Q \frac{\partial \Delta}{\partial \rho_V} / \Delta$	(357
$\frac{\partial U}{\partial n_{t}} = -B_{1}[2\eta_{t}\eta_{U} + (\eta_{Q}\rho_{V} - \eta_{V}\rho_{Q})]/\Delta - U\frac{\partial\Delta}{\partial \eta_{t}}/\Delta$	(358
$\frac{\partial U}{\partial n_0} = -B_1 [\eta_I \rho_V + \rho_V \rho_Q] / \Delta - U \frac{\partial \Delta}{\partial n_0} / \Delta$	(359
$\frac{\partial U}{\partial m_{i}} = -B_{1}[\eta_{I}^{2} + \rho_{U}^{2}]/\Delta - U\frac{\partial \Delta}{\partial m_{i}}/\Delta$	(360
$\frac{\partial U}{\partial r_{U}} = -B_{1}[-\eta_{I}\rho_{Q} + \rho_{U}\rho_{V}]/\Delta - U\frac{\partial \eta_{U}}{\partial r_{U}}/\Delta$	(361
$\frac{\partial U}{\partial x_{e}} = -B_{1}[-\eta_{I}\eta_{V} + \rho_{U}\eta_{Q}]/\Delta - U\frac{\partial \Delta}{\partial a_{e}}/\Delta$	(362
$\frac{\partial p_Q}{\partial t} = -B_1 [\eta_Q \rho_Q + \eta_u \rho_u + \eta_V \rho_V + \rho_U \eta_U] / \Delta - U \frac{\partial \Delta}{\partial t} / \Delta$	(363
$\frac{\partial \rho_U}{\partial t} = -B_1 [\eta_I \eta_O + \rho_U \eta_V] / \Delta - U \frac{\partial \Delta}{\partial t} / \Delta$	(364
$\partial \rho_V$ $\partial \rho_V$ $\partial \rho_V$	

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01	
$\frac{\partial V}{\partial \eta_I} = -B_1 [2\eta_I \eta_V + (\eta_U \rho_Q - \eta_Q \rho_U)] / \Delta - V \frac{\partial \Delta}{\partial \eta_I} / \Delta$	(365)
$\frac{\partial V}{\partial r} = -B_1 [-\eta_I \rho_V + \rho_V \rho_Q] / \Delta - V \frac{\partial \Delta}{\partial \Delta} / \Delta$	(366)
$\partial \eta_Q$ $\partial V = B \left[-\frac{1}{2} + \frac{1}{2} + \frac{1}$	(907
$\frac{\partial \eta_U}{\partial \eta_U} = -D_1 [\eta_I \rho_Q + \rho_V \rho_U] / \Delta - V \frac{\partial \eta_U}{\partial \eta_U} / \Delta$	(307
$rac{\partial V}{\partial \eta_V} = -B_1[\eta_I^2 + ho_V^2]/\Delta - V rac{\partial \Delta}{\partial \eta_V}/\Delta$	(368
$\frac{\partial V}{\partial \rho_{\mu}} = -B_1 [\eta_I \eta_U + \rho_V \eta_Q] / \Delta - V \frac{\partial \Delta}{\partial \rho_{\mu}} / \Delta$	(369
$\frac{\partial V}{\partial V} = -B_{\rm c} [-n_{\rm c}n_{\rm c} + \alpha_{\rm c}n_{\rm c}]/\Delta - V_{\rm c} \frac{\partial \Delta}{\Delta}/\Delta$	(270
$\frac{\partial \rho_U}{\partial V} = -D_1 \left[-\eta_I \eta_Q + \rho_V \eta_U \right] \Delta = \sqrt{\frac{\partial \rho_U}{\partial \rho_U}} \Delta$	(510
$\frac{\partial}{\partial \rho_V} = -B_1 [\eta_q \rho_q + \eta_U \rho_U + 2\eta_V \rho_V] / \Delta - V \frac{\partial \Delta}{\partial \rho_V} / \Delta$	(371
	(372
$\frac{\partial \Delta}{\partial \eta_I} = 2\eta_I [2\eta_I^2 - \eta_Q^2 - \eta_U^2 - \eta_V^2 + \rho_Q^2 + \rho_U^2 + \rho_V^2]$	(37:
$\frac{\partial \Delta}{\partial \eta_O} = -2\eta_I^2 \eta_Q - 2\rho_Q (\eta_Q \rho_Q + \eta_U \rho_U + \eta_V \rho_V)$	(37
$\frac{\partial \Delta}{\partial p_U} = -2\eta_I^2 \eta_U - 2\rho_U (\eta_Q \rho_Q + \eta_U \rho_U + \eta_V \rho_V)$	(37
$\frac{\partial \Delta}{\partial t} = -2n^2 n_V - 2\rho_V (n_0\rho_0 + n_0\rho_V + n_V\rho_V)$	(37
$\partial \eta_V$ $\partial \Delta$ $\partial \Delta$	(01
$\frac{\partial}{\partial \rho_Q} = 2\eta_I^* \rho_Q - 2\eta_Q (\eta_Q \rho_Q + \eta_U \rho_U + \eta_V \rho_V)$	(37
$\frac{\partial \Delta}{\partial \rho_U} = 2\eta_I^2 \rho_U - 2\eta_U (\eta_Q \rho_Q + \eta_U \rho_U + \eta_V \rho_V)$	(37
$\frac{\partial \Delta}{\partial \Delta} = 2\eta_{\mu}^2 \rho_V - 2\eta_V (\eta_0 \rho_0 + \eta_V \rho_V + \eta_V \rho_V)$	(37
$\partial \rho_V$ in the intervention of (V, V, V)	(0)
	(00
e over B	
$\partial I = {}_{t} \partial I \partial \eta_{I}$, $\partial I \partial \eta_{Q}$, $\partial I \partial \eta_{U}$, $\partial I \partial \eta_{V}$	

partial deri

imi imi

$\frac{\partial I}{\partial T} = \left[\frac{\partial I}{\partial \eta_{I}} + \frac{\partial I}{\partial \eta_{Q}} + \frac{\partial I}{\partial \eta_{$	$\rightarrow \partial I \partial \eta_V$ (28)
∂B $\partial \eta_I \partial v_B$ $\partial \eta_Q \partial v_B$ $\partial \eta_U \partial v_B$	
$+\frac{\partial I}{\partial \rho_Q} + \frac{\partial I}{\partial \rho_U} + \frac{\partial \rho_U}{\partial \rho_U} + \frac{\partial I}{\partial \rho_U} + \frac{\partial \rho_U}{\partial \rho_U}$	$I \partial \rho_{V_1} \partial v_B$ (98)
$\partial \rho_Q \partial v_B = \partial \rho_U \partial v_B = \partial \rho_U$	$\partial_V \overline{\partial v_B} \overline{\partial B}$ (38)

GOOD LUCK!

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Partial derivative over a	B ₀	
	$\frac{\partial I}{\partial B_0} = 1$	(383)
	$\frac{\partial Q}{\partial B_0} = 0$	(384)
	$\frac{\partial U}{\partial B_0} = 0$	(385)
	$\frac{\partial V}{\partial B_0} = 0$	(386)
artial derivative over B	1	
	$\frac{\partial I}{\partial B_1} = (I - B_0)/B_1$	(387)
	$\frac{\partial Q}{\partial B_1} = Q/B_1$	(388)
	$\frac{\partial U}{\partial B_1} = U/B_1$	(389)
	$\frac{\partial V}{\partial R} = V/B_1$	(390)

5.3.2. Simultaneous Fitting of Doublets

The magnetic parameters B, θ, χ and atmospheric parameters B_0, B_1 are independent of the lines. For doublets, λ_D and a are the same in both the lines.

If the central wavelength position of Fe I 6301.5 is denoted by λ_0 , then the central wavelength position of Fe I 6302.5 is $\lambda_0 + \delta \lambda$ with $\delta \lambda = 0.991$ Å.

If the ratio of the line center opacity of Fe I 6301.5 is $\eta_0,$ then that of Fe I 6302.5 is $q\eta_0$ with q=0.5.

A very important feature is that the two lines have different values of effective Lande-g factor.

Functional values

1. Free parameters: B, θ , χ , η_0 , λ_D , a, λ_0 , B_0 , B_1 among which B, η_0 , λ_D , a, B_0 , B_1 are positive definite:

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$v = \frac{\lambda - \lambda_0}{\Delta \lambda_D}, v_1 = \frac{\lambda - \lambda_0 - \delta \lambda}{\Delta \lambda_D}$	(391)
$v_B = c_0 \frac{B}{\Delta \lambda_D}, v_{B1} = r v_B$	(392)
$\phi_p = H(a, v) + qH(a, v_1)$	(393)
$\phi_r = H(a, v - v_B) + qH(a, v_1 - v_{B1})$	(394)
$\phi_b = H(a, v + v_B) + qH(a, v_1 + v_{B1})$	(395)
$\psi_p = L(a, v) + qL(a, v_1)$	(396)
$\psi_r = L(a, v - v_B) + qL(a, v_1 - v_{B1})$	(397)
$\psi_b = L(a, v + v_B) + qL(a, v_1 + v_{B1})$	(398)

(400)

(401)

(402)

(403)

(404)

(406)

5.4. Filling factor effect

2.

3.

Suppose an areal fraction α of the spatial resolution element is occupied by an unresolved magnetic structure and the rest by non-magnetic structures. Then observed Stokes parameters are given by

$$\begin{split} \boldsymbol{I} &= \alpha \boldsymbol{I}_m + (1-\alpha) \boldsymbol{I}_{nm} \\ \text{where } \boldsymbol{I}_{nm} &= (I_{nm}, 0, 0, 0). \text{ Explicitly we have} \\ & I &= \alpha I_m + (1-\alpha) I_{nm} \\ & V &= \alpha V_m \\ & Q &= \alpha Q_m \\ & U &= \alpha U_m \\ \end{split}$$
Using the weak field solution $V_m &= -CB_\parallel \frac{d(I_0)_m}{d\lambda}, \\ \text{we find} \\ & V &= \alpha V_m = -\alpha\beta CB_\parallel \frac{d(I_0)_m}{d\lambda} \\ \text{and} \end{split}$

$$(B_{\parallel})_{app} = \alpha \beta B_{\parallel}$$

STOKES INVERSI

Applying Chae's ME singlet inversion code used for Hinode/SP



B = par[0]; magnetic field strength in Gauss

theta = par[1]; inclination in radian

chi = par[2]; azimuth in radian

eta0 = par[3]; ratio of line center opacity to the continuum one

dlambdaD= par[4] ; Doppler width in angstrom

a = par[5] ; damping parameter

lambda0 = par[6]; line center in A (Doppler shift)

- BO = par[7]; zeroth order of the source function
- B1 = par[8]; first order of the source function
- I = par[9] ; intensity in ADU

SUCCESSFUL INVERSION



INVERSION FAILURE



SUCCESSFUL INVERSION WITH ADAPTIVE INITIAL GUESES



DOPPLER MAP

Chances for higher resolution velocity analysis



COMPARISON WITH SDO/HMI









Reasonable Inversion Outcome

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Fig. 1.— Unusual structures of AR 12673. (a) and (b) Hinode/SP LOS and transverse magnetic field strength. Note that in many pixels near the PIL, transverse fields are saturated at 5000 G. (c) BBSO/GST TiO image. The two white boxed in (a)–(c) mark the two strong transverse field areas at the PIL, where twisted photospheric LB structures of the δ configuration are present. (d) NIRIS Stokes U profile of a selected strong transverse field pixel at the PIL within the northern box. The direct measurement of Zeeman splitting yields a field strength of 5570 G.

Dark Structures in Sunspot Light Bridges

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Abstract

We present unprecedented high-resolution TiO images and Fe I 1565 nm spectropolarimetric data of two light bridges taken by the 1.6 m Goode Solar Telescope at Big Bear Solar Observatory. In the first light bridge (LB1), we find striking knot-like dark structures within the central dark lane. Many dark knots show migration away from the penumbra along the light bridge. The sizes, intensity depressions, and apparent speeds of their proper motion along the light bridges of 33 dark knots identified from the TiO images are mainly in the ranges of 80 \sim 200 km, 30% \sim 50%, and 0.3 \sim 1.2 km s⁻¹, respectively. In the second light bridge (LB2), a faint central dark lane and striking transverse intergranular lanes were observed. These intergranular lanes have sizes and intensity depressions comparable to those of the dark knots in LB1 and also migrate away from the penumbra at similar speeds. Our observations reveal that LB2 is made up of a chain of evolving convection cells, as indicated by patches of blueshift surrounded by narrow lanes of redshift. The central dark lane generally corresponds to blueshifts, supporting the previous suggestion of central dark lanes being the top parts of convection upflows. In contrast, the intergranular lanes are associated with redshifts and located at two sides of each convection cell. The magnetic fields are stronger in intergranular lanes than in the central dark lane. These results suggest that these intergranular lanes are manifestations of convergent convective downflows in the light bridge. We also provide evidence that the dark knots observed in LB1 may have a similar origin.

Key words: Sun: granulation - Sun: magnetic fields - Sun: photosphere - sunspots

Supporting material: animation


High-resolution observations of flare precursors in the low solar atmosphere

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Solar flares are generally believed to be powered by free magnetic energy stored in the corona¹, but the build up of coronal energy alone may be insufficient to trigger the flare to occur². The flare onset mechanism is a critical but poorly understood problem, insights into which could be gained from smallscale energy releases known as precursors. These precursors are observed as small pre-flare brightenings in various wavelengths³⁻¹³ and also from certain small-scale magnetic configurations such as opposite-polarity fluxes¹⁴⁻¹⁶, where the magnetic orientation of small bipoles is opposite to that of the ambient main polarities. However, high-resolution observations of flare precursors together with the associated photospheric magnetic field dynamics are lacking. Here we study precursors of a flare using the unprecedented spatiotemporal resolution of the 1.6-m New Solar Telescope, complemented by new microwave data. Two episodes of precursor brightenings are initiated at a small-scale magnetic channel¹⁷⁻²⁰ (a form of opposite-polarity flux) with multiple polarity inversions and enhanced magnetic fluxes and currents, lying near the footpoints of sheared magnetic loops. Microwave spectra corroborate that these precursor emissions originate in the atmosphere. These results provide evidence of low-atmospheric small-scale energy release, possibly linked to the onset of the main flare.

The long-duration 22 June 2015 M6.5 flare occurred near the disk centre (8°W, 12°N) at NOAA active region 12371. Time profiles of flare emissions in different wavelengths (including hard X-ray, soft X-ray and microwave) clearly show that shortly before the flare impulsive phase starting from ~17:51 UT, there are two short episodes of smaller-magnitude emissions at ~17:24 UT and ~17:42 UT, which we denote as P1 and P2, respectively (see Supplementary Fig. 1). We find that these emissions can only stem from the active region of the imminent M6.5 flare, and that simultaneous H α brightenings are observed with NST in the flaring core region (see Supplementary Video 1). Thus they can be regarded as precursors of the M6.5 flare. Fine-structural evolution of the associated precursor brightenings in NST H α and the surface magnetic structure are presented in Fig. 1. Specifically, the brightening associated with the precursor episode P1 first appears as a kernel, P1a, in NST at 17:23:21 UT (also discernible in ultraviolet and extreme ultraviolet; see Supplementary Fig. 2a,d), then quickly turns into an elongated structure with another kernel, P1b (Fig. 1a and Supplementary Fig. 2b). Later, from ~17:38 UT, fine-scale brightening starts to be seen in the south and travels northeastward, apparently along the previously brightened regions in P1. The precursor episode P2 starts around 17:42 UT as kernel P2a (Fig. 1b), and then another, P2b, is formed in the south (Fig. 1c). All the above brightenings exhibit little propagation towards the east. From ~17:46 UT, one of the main flare rib-



Figure 1 | Precursor brightenings. BBSO/NST chromospheric H α + 0.6 Å (**a**-**d**) and H α centre-line (**f**) images (in logarithmic greyscale) in comparison with NIRIS photospheric vertical magnetic field B_z (**e**; scaled between ±1,500 G), showing the core region structure of the 22 June 2015 M6.5 flare. Brightenings labelled P1a/P1b, P2a/P2b and Fa/Fb appear during the precursor episodes P1, P2, and at the beginning of the flare impulsive phase, respectively, the timings of which are indicated in Supplementary Fig. 1. The dashed box in **a**, **b**, **e** and **f** denotes the field of view of Figs 2b and 3a-c. The yellow contour in **e** indicates the polarity inversion line. The dashed lines in **f** illustrate sheared arcade loops L1 and L2 (also see Supplementary Fig. 2a). All the images were registered with respect to 22 June 2015 17:24 ut

High-resolution Observations of Flares in an Arch Filament System

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Abstract

We study five sequential solar flares (SOL2015-08-07) occurring in Active Region 12396 observed with the Goode Solar Telescope (GST) at the Big Bear Solar Observatory, complemented by Interface Region Imaging Spectrograph and SDO observations. The main flaring region is an arch filament system (AFS) consisting of multiple bundles of dark filament threads enclosed by semicircular flare ribbons. We study the magnetic configuration and evolution of the active region by constructing coronal magnetic field models based on SDO/ HMI magnetograms using two independent methods, i.e., the nonlinear force-free field (NLFFF) extrapolation and the flux rope insertion method. The models consist of multiple flux ropes with mixed signs of helicity, i.e., positive (negative) in the northern (southern) region, which is consistent with the GST observations of multiple filament bundles. The footprints of quasi-separatrix layers (QSLs) derived from the extrapolated NLFFF compare favorably with the observed flare ribbons. An interesting double-ribbon fine structure located at the east border of the AFS is consistent with the fine structure of the QSL's footprint. Moreover, magnetic field lines traced along the semicircular footprint of a dome-like QSL surrounding the AFS are connected to the regions of significant helicity and Poynting flux injection. The maps of magnetic twist show that positive twist became dominant as time progressed, which is consistent with the injection of positive helicity before the flares. We hence conclude that these circular shaped flares are caused by 3D magnetic reconnection at the OSLs associated with the AFS possessing mixed signs of helicity.

Key words: Sun: chromosphere - Sun: corona - Sun: evolution - Sun: filaments, prominences - Sun: flares - Sun: magnetic fields

Supporting material: animations



Figure 9. GST/TiO images (first column) and photospheric magnetograms observed by HMI (second column) and GST (third column) at 18:04 UT (top row) and 22:36 UT (bottom row). Significant flux cancellations occur in the region enclosed by black and white boxes.

ARTICLE

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Transient rotation of photospheric vector magnetic fields associated with a solar flare

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As one of the most violent eruptions on the Sun, flares are believed to be powered by magnetic reconnection. The fundamental physics involving the release, transfer, and deposition of energy have been studied extensively. Taking advantage of the unprecedented resolution provided by the 1.6 m Goode Solar Telescope, here, we show a sudden rotation of vector magnetic fields, about 12–20° counterclockwise, associated with a flare. Unlike the permanent changes reported previously, the azimuth-angle change is transient and cospatial/ temporal with H α emission. The measured azimuth angle becomes closer to that in potential fields suggesting untwist of flare loops. The magnetograms were obtained in the near infrared at 1.56 µm, which is minimally affected by flare emission and no intensity profile change was detected. We believe that these transient changes are real and discuss the possible explanations in which the high-energy electron beams or Alfve'n waves play a crucial role.





Fig. 3 Temporal evolution of azimuth angle deviation. **a** Azimuth angle map taken before the flare at 17:32:35 UT. Three slits are put on the regions of interest (R1-3), plus a reference region in the lower right corner. The white contours outline the sunspot umbral areas (>1800 G). **b** The curves with error bars are the temporal variation of averaged azimuth angle within regions of R1-3. The uncertainties are estimated using the standard deviation of the preflare data points. The peaks are more than three times of the uncertainties rendering themselves statistically significant. The flare time is determined by the H α light curve, for instance, the dashed line is the H α light curve of R3, in which the peak matches with azimuth angle peak in R3. All H α light curves are in natural log space and self-normalized to their peak emission. In the bottom, the temporal variation of the azimuth angle in the reference region is plotted, which is manually increased by 50° to match the plotting range (50-190°). The dotted-dash curves are the azimuth angles of extrapolated potential fields that remain certain levels above the azimuth angles of real fields. **c** Temporal variation of averaged magnetic flux strength within the representative areas. **d** Temporal variation of averaged inclination within the representative areas



Fig. 5 Stokes profiles before and during the flare. Stokes components (I, Q, U, and V) taken near R3 before (blue) and during (pink) the flare. a Stokes I. b Stokes Q. c Stokes U. d Stokes V. It is clear that the Stokes I and V components remain almost unchanged but Q and U components are significantly affected during the flare

FUTURE PLAN

SIR inversion code for more scrutinized analysis of the magnetic fields

Machine learning for inversion for better accuracy and scaling with high processing speed

10830 polarimetry will be operational next summer

THANK YOU!